

Midlatitude Ocean-Atmosphere Model: Decadal Variability and Dynamics

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Plan of the Presentation

(1) Statement of the problem and background

(2) Midlatitude ocean-atmosphere model

(3) Low-frequency variability patterns

(4) Role of the oceanic eddies

Papers

Berloff, P., S. Kravtsov,, W. Dewar, and J. McWilliams, 2006: Ocean eddy dynamics in a coupled ocean-atmosphere model. *J. Phys. Oceanogr.*, submitted.

Kravtsov, S., P. Berloff, W. Dewar, M. Ghil, and J. McWilliams, 2006b: A highly nonlinear coupled mode of decadal-to-interdecadal variability in a mid-latitude ocean-atmosphere model. Part II: Dynamics. *J. Climate*, submitted.

Kravtsov, S., W. Dewar, P. Berloff, J. McWilliams, and M. Ghil, 2006a: A highly nonlinear coupled mode of decadal-to-interdecadal variability in a mid-latitude ocean-atmosphere model. Part I: Phenomenology. *J. Climate*, submitted.

Statement of the Problem

- The **central hypothesis** is:

In the midlatitudes, the ocean-atmosphere system generates a *coupled* low-frequency variability (LFV) mode.

- The **main questions** are:

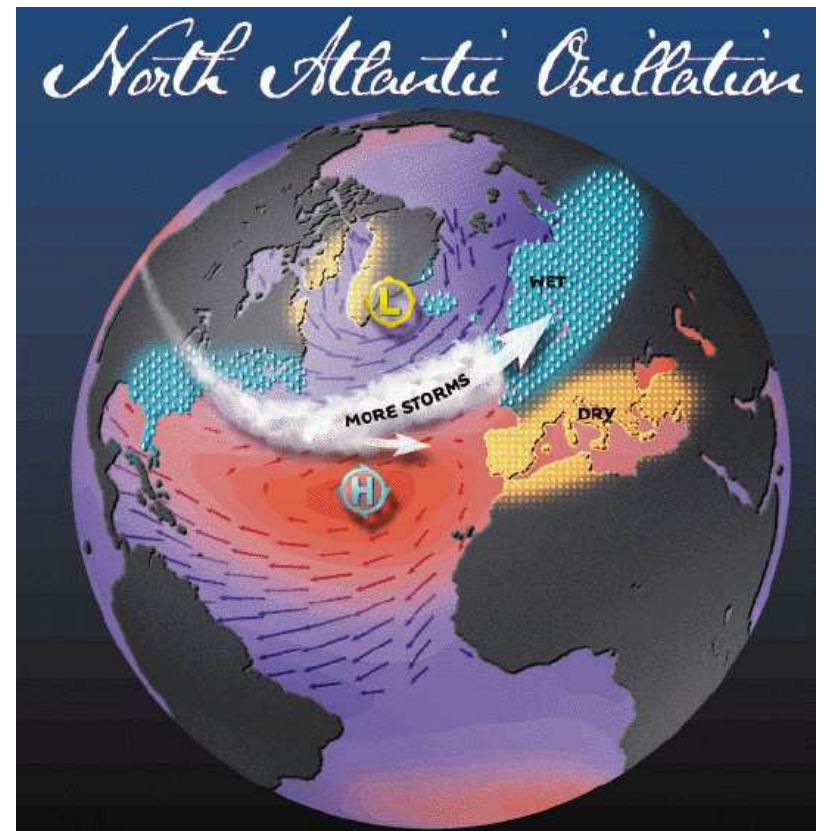
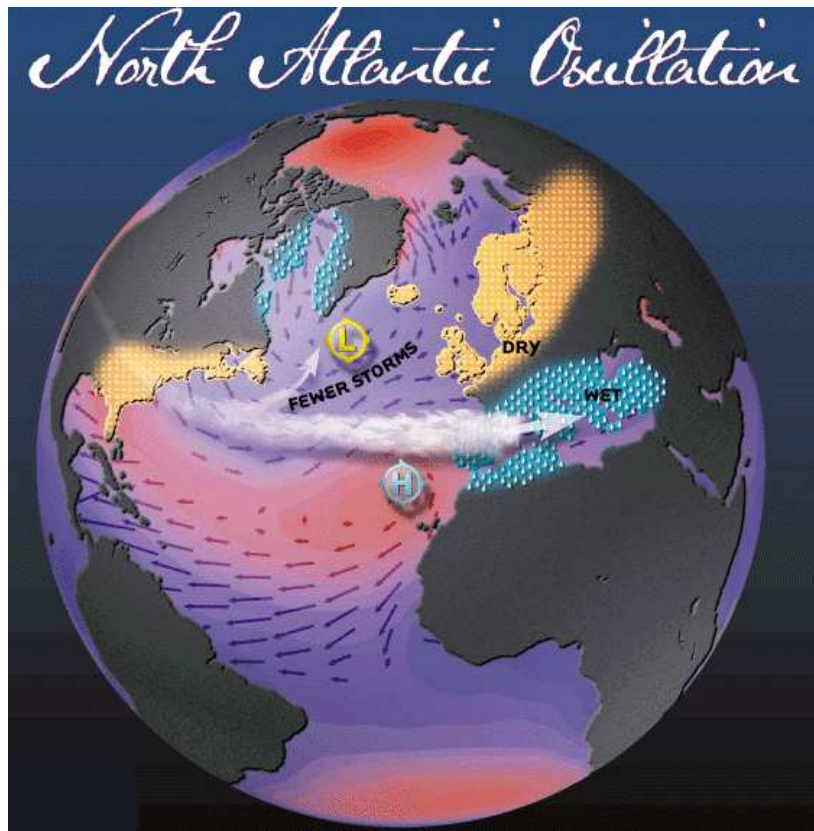
(1) What is the generic LFV pattern?

(2) What is the underlying dynamical mechanism?

(3) What is the effect of the mesoscale oceanic eddies and how to parameterize it?

1. Background: Observations

- In the equatorial ocean, there is a well-known coupled interannual oscillation: *El Nino*.
- In the North Pacific and North Atlantic, *decadal variability is observed both in the ocean and atmosphere (below, opposite phases of the NAO pattern are shown).*



2. Background

- Dynamical mechanism of the decadal LFV in middle latitudes remains a mystery, and it can be explained as:
 - (i) *Intrinsic atmospheric*,
 - (ii) *Intrinsic oceanic*,
 - (iii) *Coupled ocean-atmosphere* mechanism.
- Comprehensive ocean-atmosphere GCMs do not yet discriminate between the above options, because:
 - (a) Dynamics in GCMs is rather difficult to analyze;
 - (b) Oceanic mesoscale eddies in GCMs are not properly resolved and, instead, are inaccurately parameterized.
- *Idealized coupled models* are the analytical tool of choice, but their hierarchy is so far incomplete and poorly studied.

3. Background: Intrinsic Variability Studies

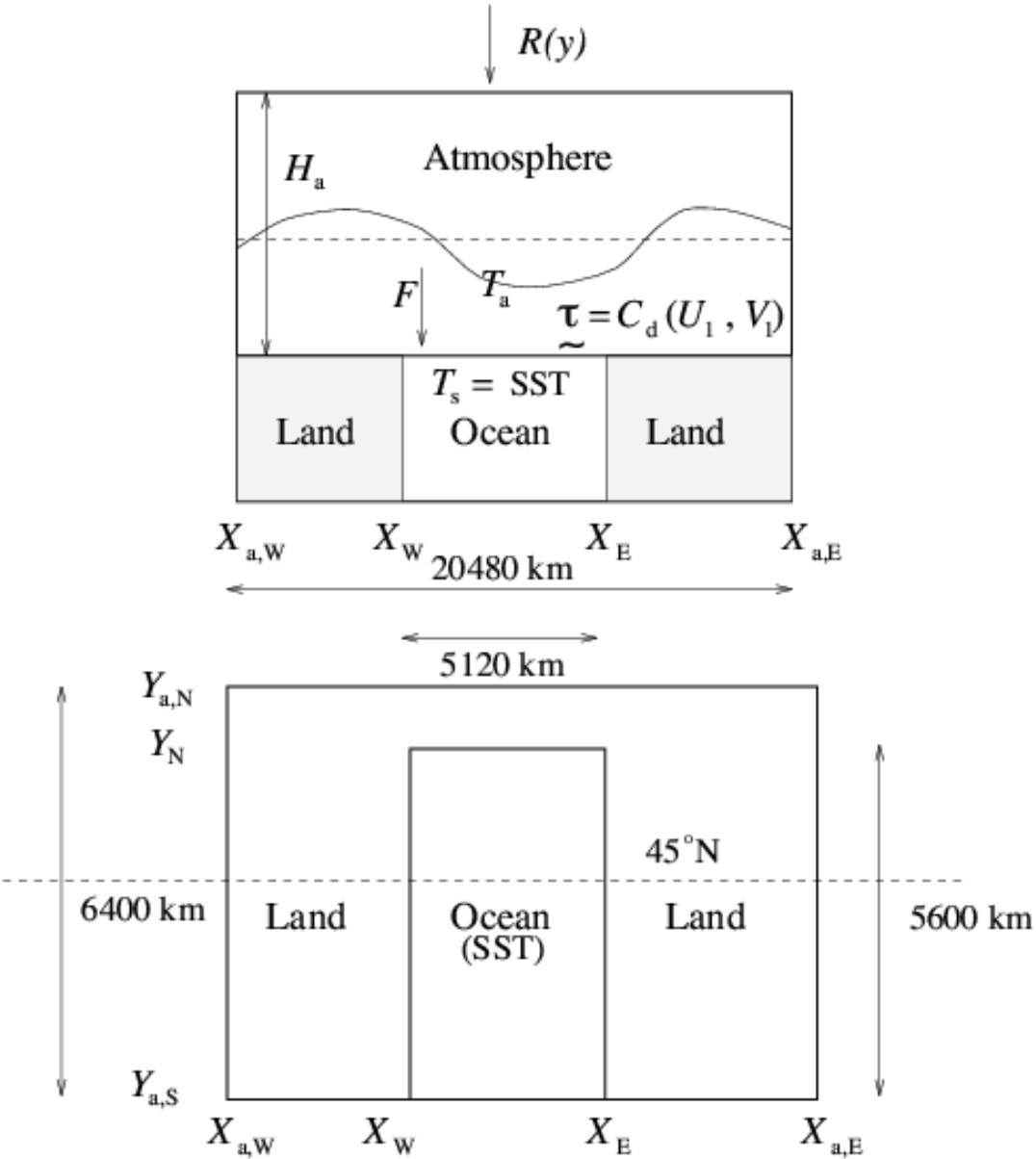
- *Atmospheric*, intrinsic decadal LFV is a poorly understood phenomenon:
 - It can be related to bimodality of the atmosphere (Kravtsov et al. 2005).
- *Oceanic*, intrinsic decadal LFV is understood much better (in the context of steady atmospheric forcing!), and there are 2 classes of the dynamical mechanisms proposed:
 - The “linear” school of thought explains this variability in terms of the linear unstable eigenmodes and early bifurcations of the underlying nonlinear steady state (e.g., *works by Drs Michael Ghil, Henk Dijkstra and their collaborators*);
 - An alternative idea is that the LFV is a fundamentally turbulent phenomenon that invokes (1) energetic mesoscale eddies and (2) inhibited (i.e., non-diffusive) eddy transport between the oceanic gyres (e.g., *Berloff et al. 2006*).

This talk focuses on the COUPLED ocean-atmosphere case...

4. Background: Coupled Models

- In the coupled ocean-atmosphere models, imposed spatial resolution of the ocean is a major problem (i.e., *the atmosphere is always over-resolved compare to the ocean*):
 - The typical, $4^\circ \times 4^\circ$, ocean resolution is equivalent to 4×4 points resolution of the atmosphere;
 - The adequate resolution constraint can be relaxed by using an idealized ocean dynamics.
- The following types of the idealized ocean component have been looked at:
 - Linear;
 - With nonlinear thermohaline circulation;
 - With nonlinear horizontal circulation, but not in the turbulent regime;
 - **Fully turbulent regime** of the horizontal circulation [*this study*].
- For this purpose, quasigeostrophic (QG) coupled models are a very useful tool!
 - They have been formulated recently (Kravtsov and Robertson 2002; Hogg et al. 2003), and their analysis is in progress;
 - The QG approximation filters out the (unbalanced) fast motions and yields evolution of the (balanced) geostrophic currents.

Model Configuration: Atmosphere, Ocean, and Oceanic Mixed Layer



1. Atmosphere Component: Fluid Dynamics

- The barotropic and baroclinic potential vorticities (ψ and τ are the corresponding velocity streamfunctions; Rd is the Rossby deformation radius) are:

$$q_\psi = \nabla^2 \psi + \beta y, \quad q_\tau = \nabla^2 \tau - Rd^{-2} \tau$$

- The isopycnal-layer velocity streamfunctions (h_1 and h_2 are the layer depths) are:

$$\psi_1 = \psi + h_2 \tau, \quad \psi_2 = \psi - h_1 \tau$$

- The governing equations:

$$\frac{\partial q_\psi}{\partial t} + J(\psi, q_\psi) = -h_1 h_2 J(\tau, q_\tau) - k \left[\nabla^2 \psi + h_2 \nabla^2 \tau \right] - \sum_{n=1}^3 k^{(n)} \nabla^2 \psi^{(n)} + A_H \nabla^6 \psi$$

$$\begin{aligned} \frac{\partial q_\tau}{\partial t} + (h_2 - h_1) J(\tau, q_\tau) = & - \left[J(\tau, q_\psi) + J(\psi, q_\tau) \right] + \frac{f_0}{H_a} \frac{1}{h_1 h_2} F(\mathbf{x}; \psi, \tau) \\ & - k \left[\frac{h_2}{h_1} \nabla^2 \tau + \frac{1}{h_1} \nabla^2 \psi \right] - \sum_{n=1}^3 k^{(n)} \nabla^2 \tau^{(n)} + A_H \nabla^6 \tau \end{aligned}$$

- Re-entrant zonal channel with the no-slip velocity condition on the boundaries.
- Mass and momentum constraints (McWilliams 1977).

2. Atmosphere Component: Radiation and Heat Exchange

- Atmospheric temperature, T_a , is the average temperature of an air column:

$$T_a = T_{eq} - C \tau$$

- The atmosphere is transparent to the short-wave solar radiation:

$$R(y) = 190 - 165 \sin\left(\frac{2y}{r}\right) \quad \left[Wm^{-2}\right]$$

- The following functions depend on T_a , sea surface temperature (SST), and some parameters:

O — oceanic long-wave radiation (absorbed by the atmosphere);

B — atmospheric back radiation;

H_{SL} — sensible and latent ocean-atmosphere heat exchange (also depends on the sea-level wind speed).

- Over the *ocean*, the atmospheric forcing function is:

$$F \sim O + H_{SL} - 2B,$$

and over the *land*, it is:

$$F \sim R - B.$$

1. Ocean Component

- The isopycnal-layer potential vorticities and streamfunctions are connected as:

$$\begin{aligned} Q_1 &= \nabla^2 \Psi_1 + \frac{f_0^2}{g'_1 D_1} (\Psi_2 - \Psi_1) + \beta y, \\ Q_2 &= \nabla^2 \Psi_2 - \frac{f_0^2}{g'_1 D_2} (\Psi_2 - \Psi_1) + \frac{f_0^2}{g'_2 D_2} (\Psi_3 - \Psi_2) + \beta y, \\ Q_3 &= \nabla^2 \Psi_3 - \frac{f_0^2}{g'_2 D_3} (\Psi_3 - \Psi_2) + \beta y, \end{aligned}$$

where g'_i and D_i are the reduced gravities and the layer thicknesses.

- The governing equations are:

$$\begin{aligned} \frac{\partial Q_1}{\partial t} + J(\Psi_1, Q_1) &= \frac{f_0}{D_1} (W_E - W_D) + \nu \nabla^4 \Psi_1, \\ \frac{\partial Q_2}{\partial t} + J(\Psi_2, Q_2) &= \frac{f_0}{D_2} W_D + \nu \nabla^4 \Psi_2, \\ \frac{\partial Q_3}{\partial t} + J(\Psi_3, Q_3) &= -\gamma \nabla^2 \Psi_3 + \nu \nabla^4 \Psi_3, \end{aligned}$$

where the Ekman pumping, W_E , and the entrainment rate, W_D , are both obtained from the mixed-layer dynamics and thermodynamics.

2. Ocean Component

- Rectangular-shape basin and flat bottom.
- Partial-slip lateral boundary condition: $\alpha \Psi_{nn} - (1 - \alpha/L) \Psi_n = 0$
- Mass conservation constraint:

$$\frac{\partial}{\partial t} \iint (\Psi_1 - \Psi_2) dx dy = \frac{f_0}{g'_1} \iint W_D dx dy; \quad \frac{\partial}{\partial t} \iint (\Psi_2 - \Psi_3) dx dy = 0$$

(only the first layer interface is affected by the entrainment).

- Lateral eddy diffusivity accounts for dynamically unresolved submesoscale eddies.

Mixed Layer Component

- Surface stress is calculated from the wind: $\tau^{(x)} \sim k(U - V)$, $\tau^{(y)} \sim k(U + V)$
- Mixed-layer velocity is the sum of the geostrophic and Ekman components:

$$u = -\frac{\partial \Psi_1}{\partial y} + \frac{1}{\rho_o} \frac{\tau^{(y)}}{f_0 h_{mix}}, \quad v = \frac{\partial \Psi_1}{\partial x} - \frac{1}{\rho_o} \frac{\tau^{(x)}}{f_0 h_{mix}}$$

- The corresponding Ekman pumping is:

$$W_E = h_{mix} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right)$$

- SST evolves according to:

$$\frac{\partial T_s}{\partial t} + \frac{\partial}{\partial x}(u T_s) + \frac{\partial}{\partial y}(v T_s) - \frac{1}{h_{mix}} W_E T_s = \frac{(F_s + F_{entr})}{\rho_o c_{P,o} h_{mix}} + K_H \nabla^2 T_s$$

— Surface heat flux, F_s , is a linear function of T_a and T_s ;

— Entrainment heat flux through the base of the mixed layer, F_{entr} , is parameterized and $W_D \sim F_{entr}$.

Let's take a close look at the reference ocean-atmosphere solution...

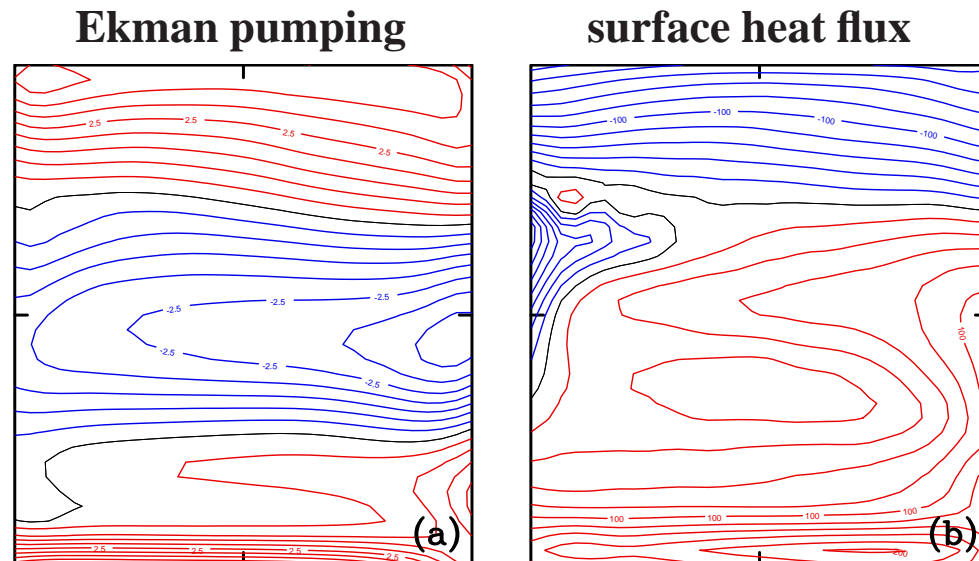
Time-Mean Forcing of the Ocean

- Wind curl imposes the triple-gyre structure.
- Sequential drift of solutions is prohibited by imposing:

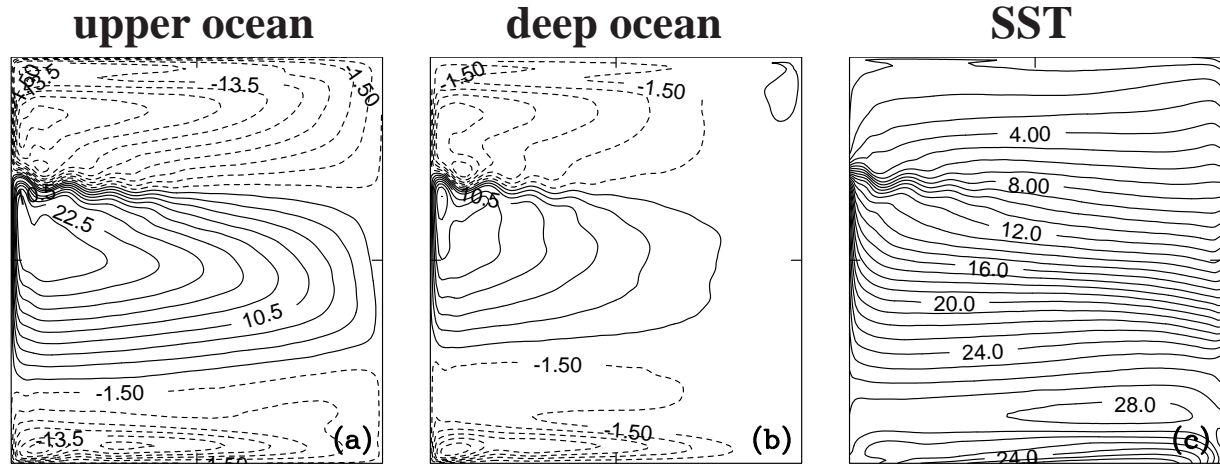
$$\iint W_D(x, y, t) dx dy = 0.$$

— In the real ocean this is achieved by the thermohaline circulation.

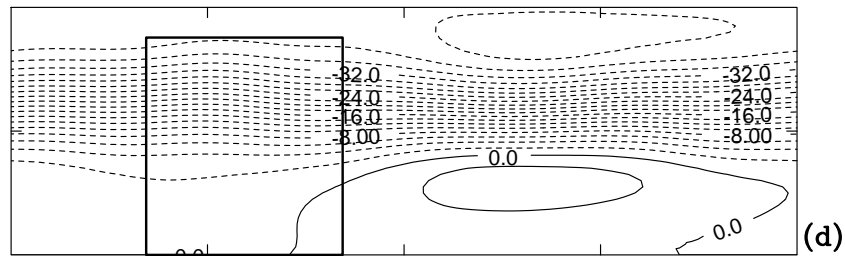
- The surface heat flux reaches 150 W m^{-2} (moderate strength).
- *The decadal LFV is associated with strong changes of the Ekman pumping and surface heat flux patterns.*



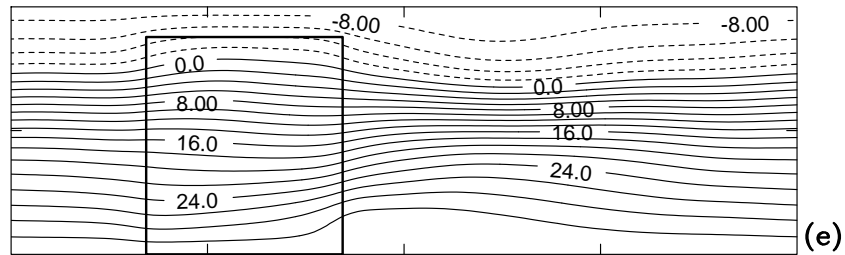
Time-Mean Fields: Ocean, Mixed Layer, and Atmosphere



barotropic streamfunction



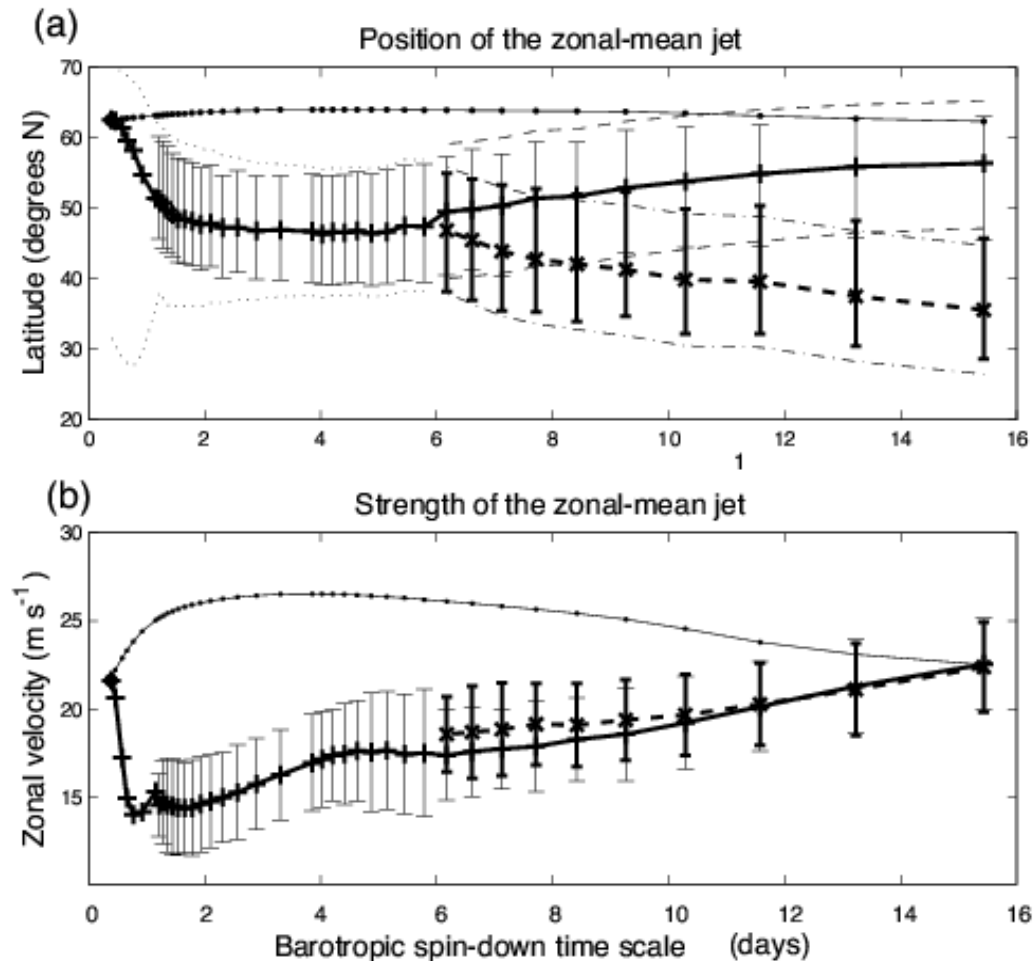
temperature



How does the atmosphere behave with the time-mean SST imposed?

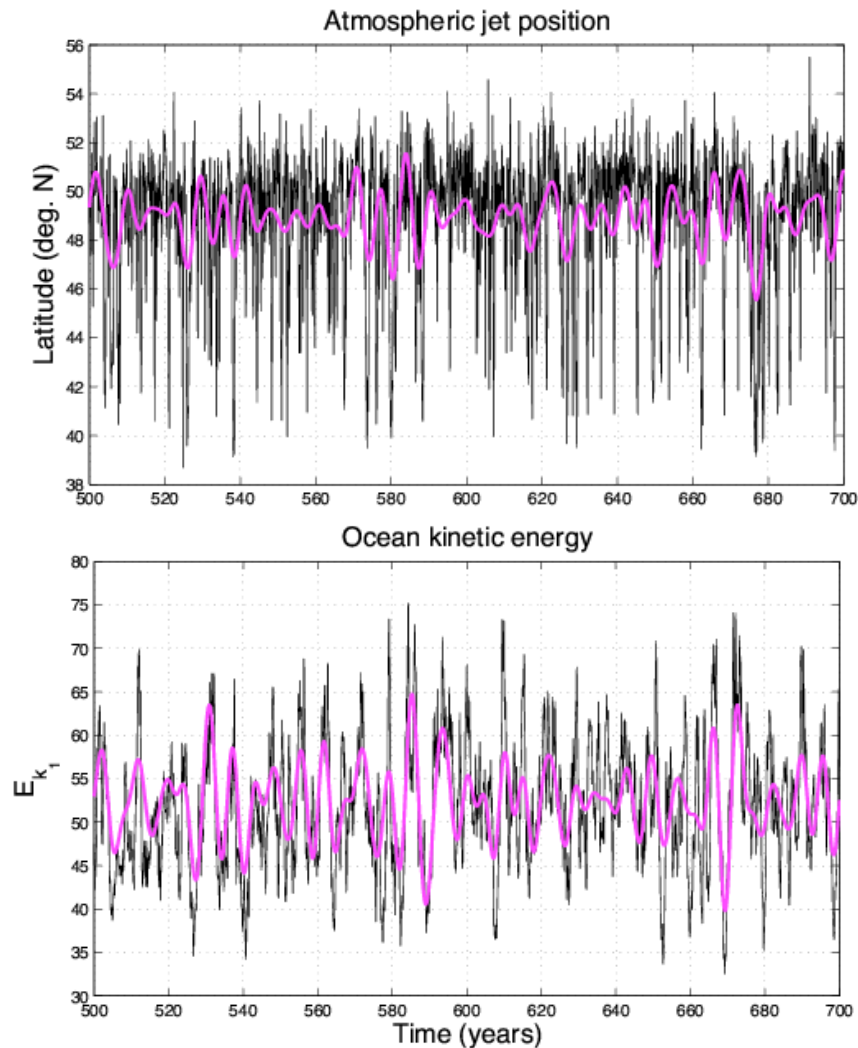
Bimodal Atmosphere

- Depending on the surface drag, k , the atmosphere can have two statistically preferred zonal states (Kravtsov et al. 2005):
 - There are rare and irregular transitions between these states;
 - The underlying unstable steady state is dynamically irrelevant.



1. Temporal Variability: Time Series

- Although, high-latitude (*HL*) state of the atmosphere is more persistent, there are systematic transitions to the low-latitude (*LL*) state.
 - Decadal variability is associated with modulation of the frequency of transitions.

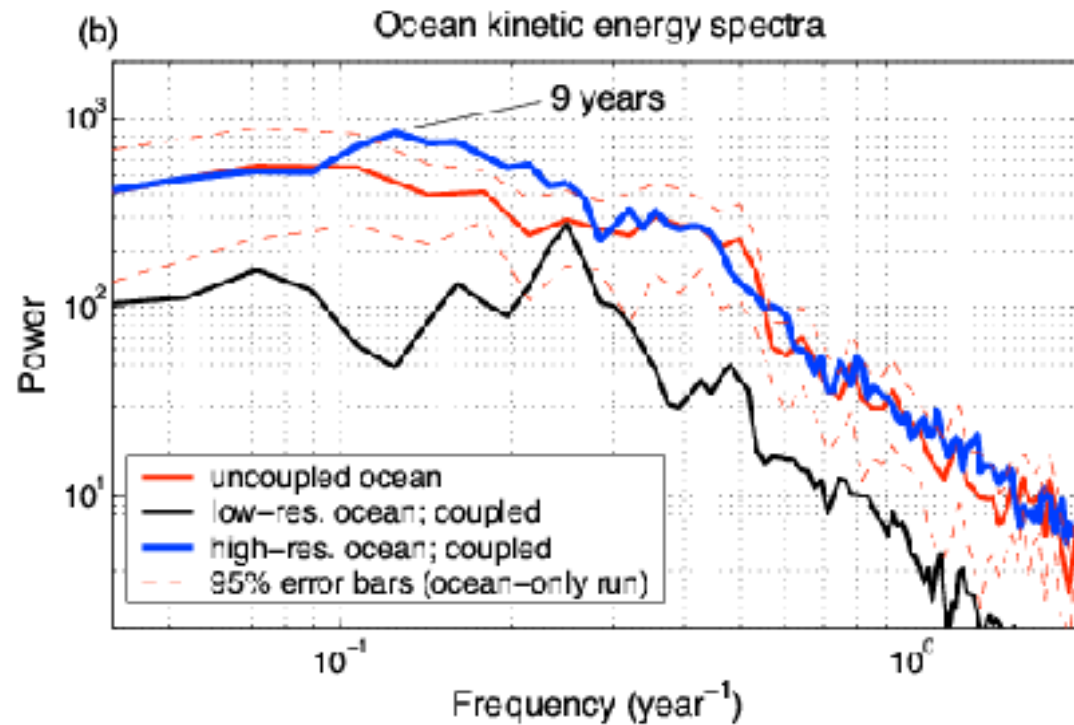


Is this variability coupled?

Is it a large- Re phenomenon?

2. Temporal Variability: Power Spectra

- Significant fraction of decadal variability has both **coupled** and **large-Re** origins.

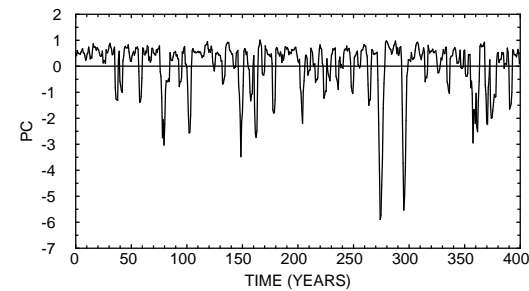
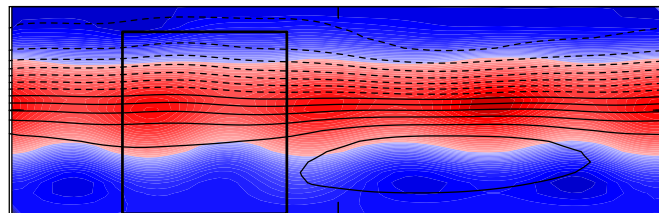


How do the atmosphere and ocean LFV patterns look like?

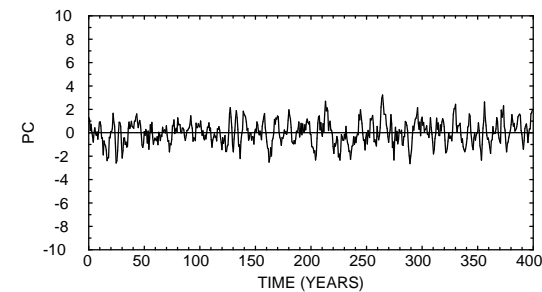
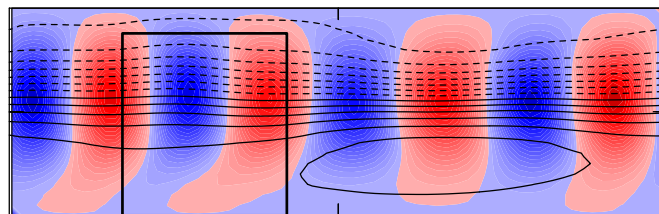
Atmosphere Variability Patterns

- Empirical Orthogonal Functions (EOFs) and their principal components show that most of the atmospheric LFV is due to **decadal meridional shifts** of the mean jet stream.
 - The rest of the signal is dominated by the 4-year propagating mode.

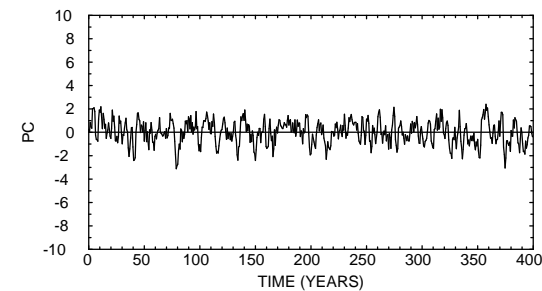
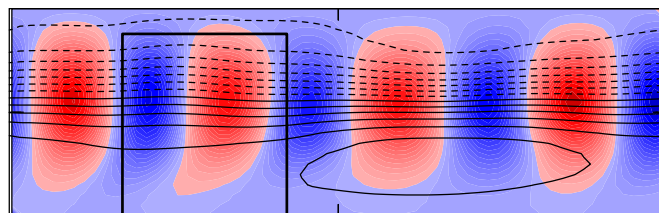
EOF=1; variance=64.1%



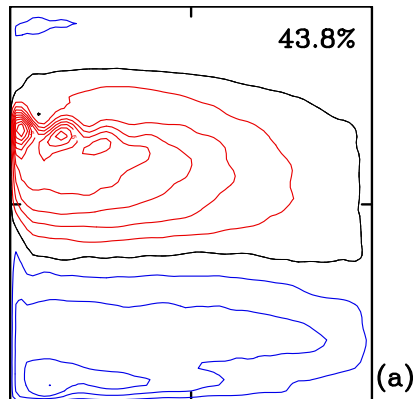
EOF=2; variance=17.6%



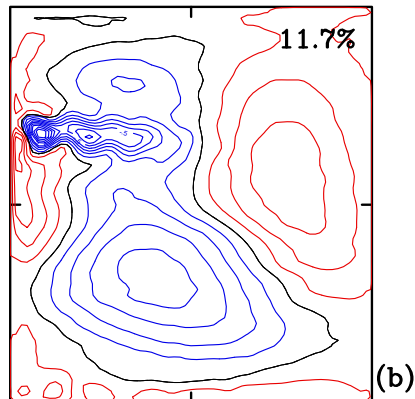
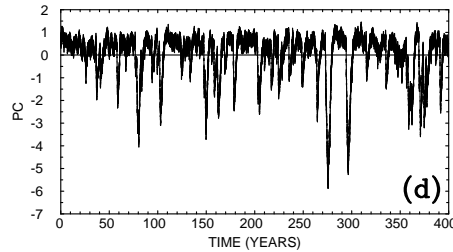
EOF=3; variance=14.9%



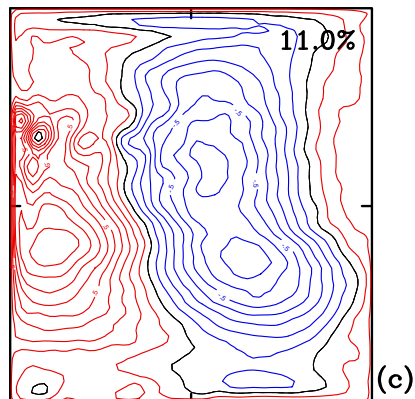
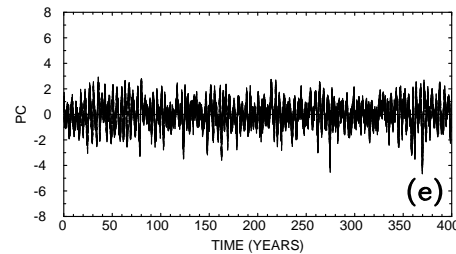
Ocean Variability Patterns



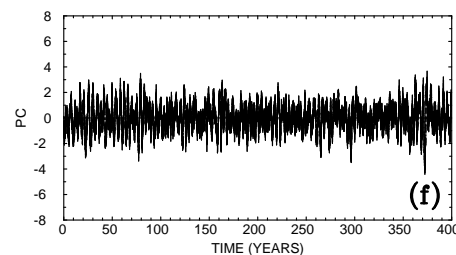
EOF=1: shifting mode



EOF=2: basin mode



EOF=3: basin mode

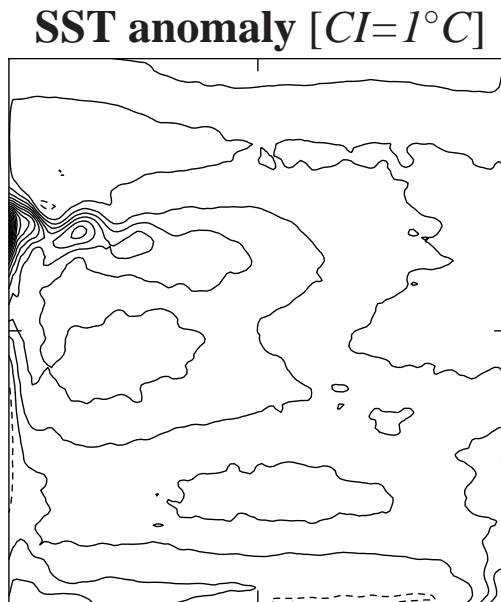


- Variability of the atmosphere projects on variability of the ocean forcing.
 - Ekman pumping, W_E , reshapes the main gyres (*active* role);
 - Entrainment rate, W_D , tends to spin the gyres down (*passive* role).
- Ocean variability is dominated by **decadal shifts** and 4-year basin mode.
 - The latter is a linear coupled phenomenon (Goodman & Marshall 1999).

Is the decadal shifting mode coupled?

SST Variability and Its Effect on the Atmosphere

- Ocean shift from the *HL* to *LL* state is associated with substantial cooling of the mixed layer.



The key question:

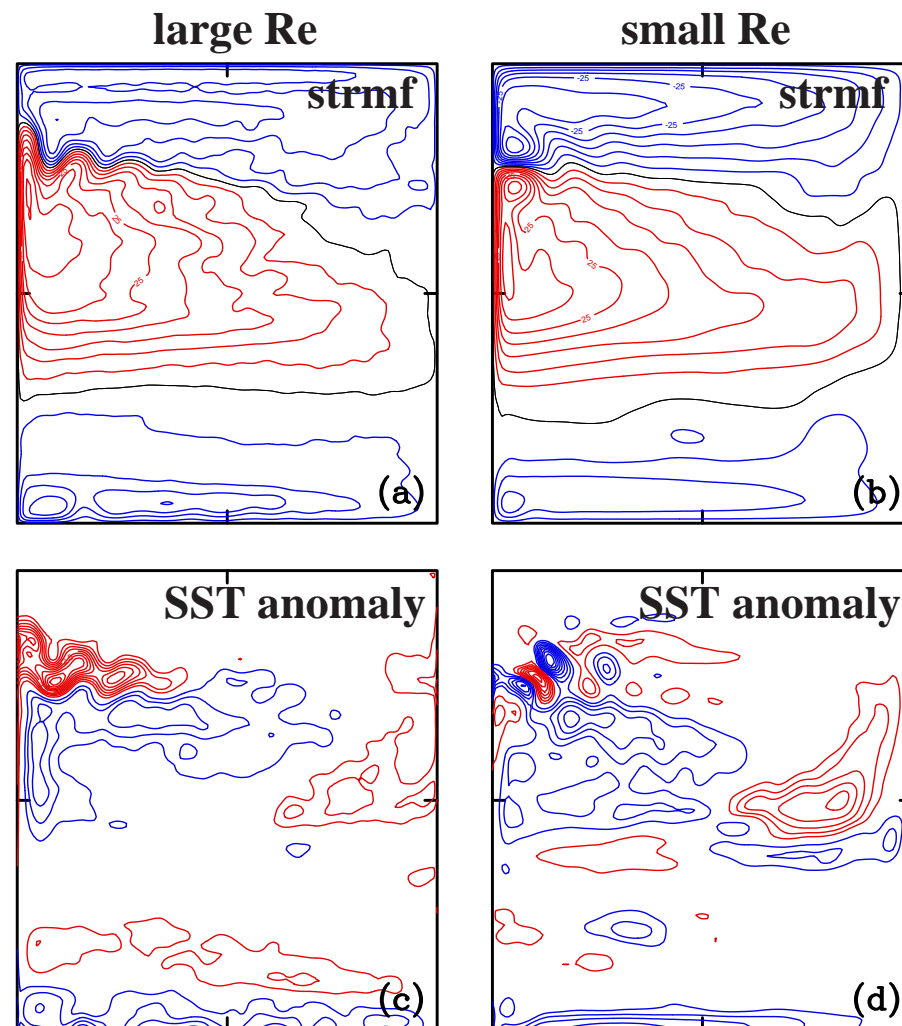
Does the OCEANIC contribution to this SST anomaly have an effect on the atmosphere?

- The answer is given by solving for the Atmosphere/Mixed-Layer (*A+ML*) combined system which is decoupled from the underlying ocean. For this purpose:
 - Conditionally-averaged ocean states are found for several phases of the shifting mode;
 - These states are kept fixed below the mixed layer;
 - The corresponding *A+ML* solutions are found.
- For different phases of the ocean, probability of the atmospheric transitions between the *HL* to *LL* states varies by 10%.
By changing this probability, ocean always tends to push atmosphere to the opposite state.

Oceanic Nonlinear Adjustment sets decadal timescale of the LFV (Dewar 2003).

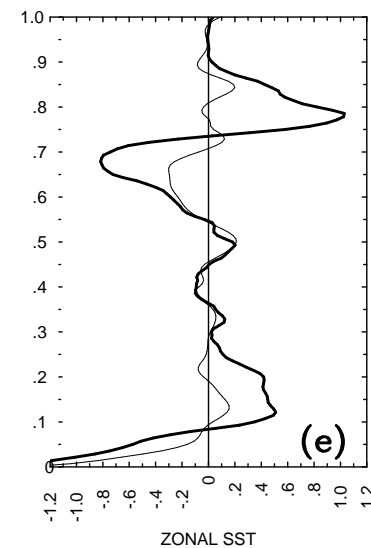
Ensemble-averaged ocean states that are nearly adjusted to the HL state are shown below.

- If the eddies are not resolved, adjustment is different and effect on the atmosphere is lost:



- Adjustment to each state yields *long-term SST anomalies*;
- These anomalies force atmosphere toward the opposite state only in the large-*Re* case.

zonal mean anomaly



Dependence of the LFV on the Model Parameters

- Weaker oceanic **bottom friction** yields longer oceanic adjustment timescale and, therefore, slower LVF.
 - The variability can be even *interdecadal*;
 - The dynamical mechanism remains the same.
- **Atmospheric surface drag** must be in the intermediate range:
 - *Weak* surface drag makes atmospheric bimodality too intermittent (i.e., probability of atmospheric transition to the opposite state becomes too small), therefore oceanic feedback on the atmosphere becomes inefficient;
 - *Strong* surface drag makes the atmosphere unimodal—this degrades sensitivity of the atmosphere to the SST anomalies.
- **Reynolds number** must be large (unless eddy effects are accurately parameterized).

How do the oceanic eddies drive the coupled mode?

Let's isolate the eddies and their effects...

1. Eddy Diagnostics

- Coarse-grained ocean solution can be decomposed into the large-scale and eddy components,

$$\mathbf{u} = \bar{\mathbf{u}} + \mathbf{u}' \quad q = \bar{q} + q',$$

in the *dynamically consistent* way (Berloff 2005), in order to analyze eddy effects.

- For this purpose:

(1) Governing equations are re-written on a coarse grid;

(2) Solution of the coarse-grid model defines $\bar{\mathbf{u}}$, and the eddies, \mathbf{u}' , are found as the residual;

(3) The coarse-grid model is driven by both the *atmospheric forcing* history and the *eddy-forcing* correction;

(4) The eddy-forcing correction is calculated interactively as the difference between the coarse-grid predicted and true nonlinearities;

(5) In terms of the flow components, the eddy forcing can be found as

$$f(t, \mathbf{x}) = -\nabla(\bar{\mathbf{u}} q' + \mathbf{u}' \bar{q} + \mathbf{u}' q'),$$

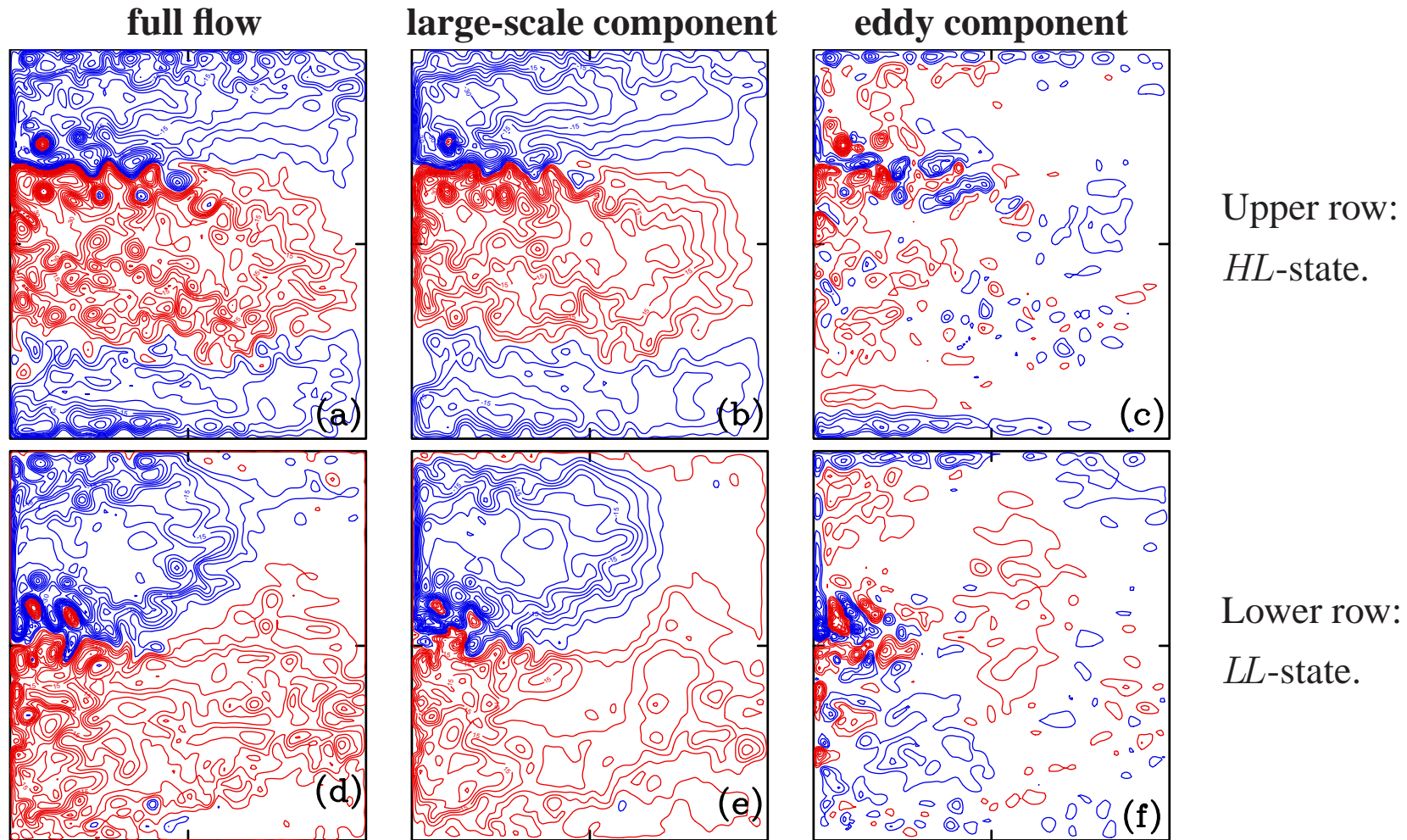
where ∇ is the coarse-grid operator and state variables are taken on the coarse grid.

- Eddy forcing consists of the relative-vorticity and stretching components associated with:

$$q = R + B; \quad R = \nabla^2 \psi, \quad B = \frac{\partial}{\partial z} S \frac{\partial \psi}{\partial z}$$

2. Eddy Diagnostics: Illustration

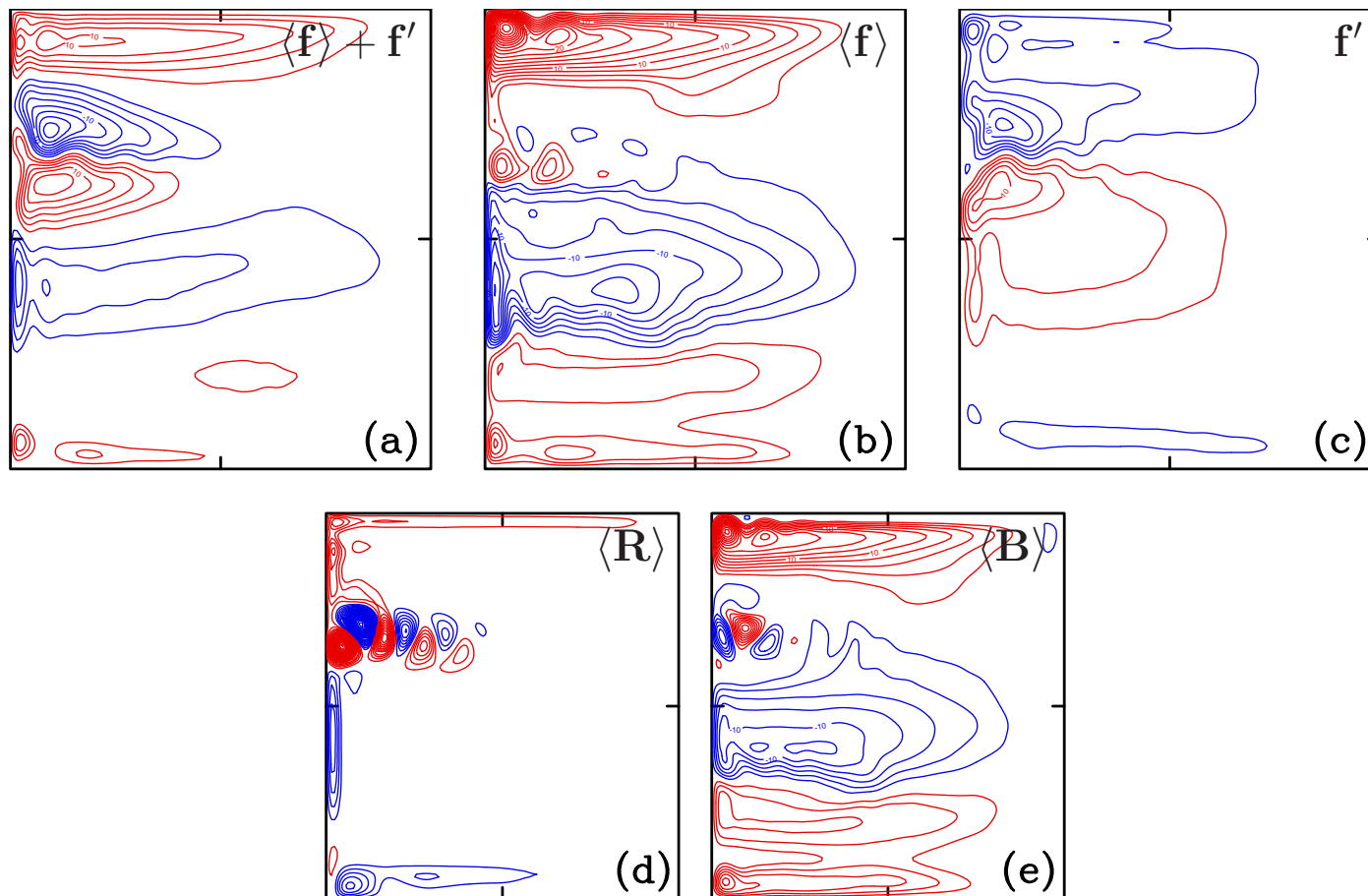
- The algorithm ensures that coarse-grid solution approximates the full solution (*typical flow snapshots are shown below*).



What is the dynamical role of the eddy forcing? Which components of it are important?

Dynamical Response to the Eddy Forcing

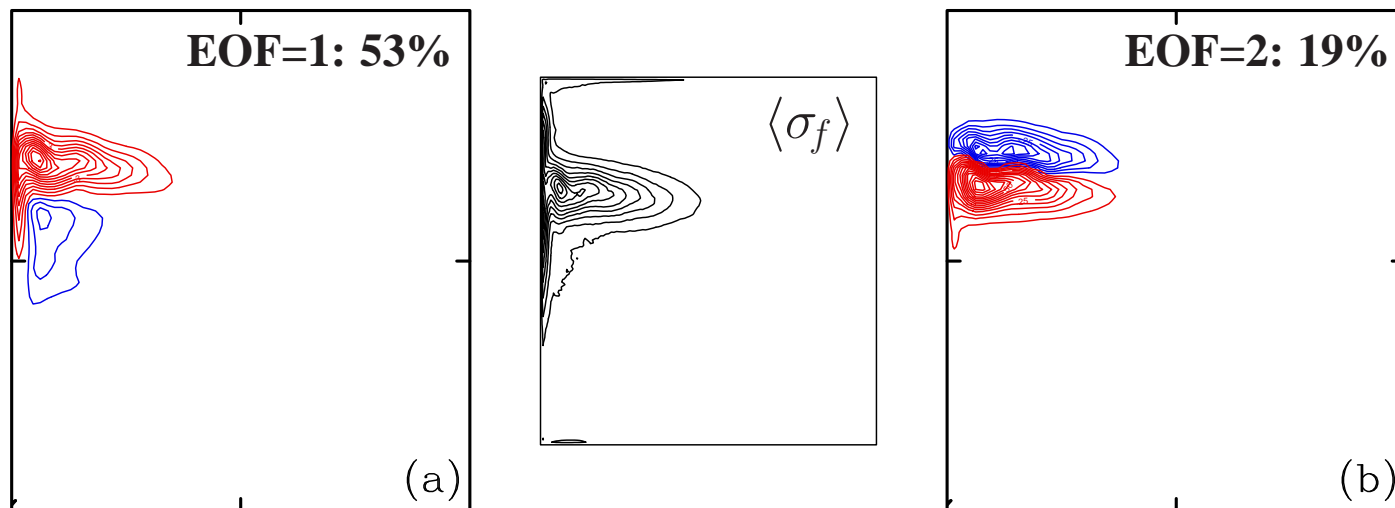
- The eddy forcing, $f(t, \mathbf{x}) = \langle f(\mathbf{x}) \rangle + f'(t, \mathbf{x})$, weakens the upper-ocean gyres and enhances the eastward jet:
 - The former effect is due to the $\langle B \rangle$ -forcing [*baroclinic instability*];
 - The latter effect [*rectification*], which is fundamentally important for the coupled variability, is due to the f' -forcing (mostly its R' component).



Variance of the Eddy Forcing

The f' -forcing is characterized by its variance...

- This variance, $\sigma_f(t, \mathbf{x})$, is *non-stationary*, and its variability is recovered by splitting eddy forcing into the low- and high-passed frequency components.
- Contribution of the leading EOF of $\sigma_f(t, \mathbf{x})$ is highly correlated with the coupled shifting mode (*the two leading EOFs and the time-mean pattern are shown below*).
 - It is an essential part of the LFV, because it controls adjustments of the eastward jet.



Let's summarize what we've learned so far about the LFV mechanism...

Mechanism of the Coupled Variability

★ *Essential aspects:*

- (i) **Bimodality** of the atmosphere allows for natural transitions between the preferred zonal states.
- (ii) Oceanic **mesoscale eddies** maintain the eastward jet through the anti-diffusive nonlinear rectification process.

★ The LFV cycle involves the following:

- (1) Changes of the frequency of atmospheric transitions can induce an oceanic transition from one preferred state to the other.
- (2) This transition is a slow nonlinear adjustment process involving complex interaction between the eastward jet and mesoscale eddies — it sets decadal-to-interdecadal timescale of the variability.
- (3) SST anomalies associated with the oceanic adjustment modulate frequency of atmospheric transitions and reverse the cycle.

Is there a simple mathematical model for the effect of the eddies?

Coupled Ocean-Atmosphere Model with Random Eddies

- We model the eddy effects in a non-eddy-resolving model in terms of space-time correlated **random** forcing fields (Berloff 2005).

— The random forcing, like the actual eddies, induces rectification of the oceanic eastward jet.

- Non-stationary variance of the random forcing is *required*, otherwise ocean solutions are trapped in the more preferred *HL* state.

- We found a simple **parameter closure**: the non-stationary random-forcing variance is related to the oceanic baroclinicity index,

$$I_{BC} = \iint (\Psi_1 - \Psi_2) dx dy ,$$

which is integrated over the area surrounding the eastward jet.

- ★ The randomly forced coupled model generates correct low-frequency coupled variability although it does not resolve the eddies — **MODELLING SUCCESS!**

Summary

(0) Coupled quasigeostrophic ocean-atmosphere model has astonishingly rich dynamics—it is a powerful tool for analysis of interactions between climate variability and turbulence.

Use it!

(1) Solutions of the turbulent ocean-atmosphere model are analyzed and decadal coupled variability is found for a wide range of physical parameters.

(2) Both the variability mechanism and the fundamental role of the oceanic eddies are understood in terms of the basic fluid mechanics.

(3) The eddy effects are modeled (parameterized) in terms of non-stationary stochastic process with parameters related to the large-scale flow pattern.